



## How to Build Smarter Decision Models Capable To Make Optimal Decisions

Jacob Feldman, PhD OpenRules, Inc., CTO www.openrules.com

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### **Decision Management Tools**

www.decision-tools.org

Software Tools for Decision Management

Tool Catalogues Decision Model Collection

This website maintains Live Catalogues of Decision Management Software currently available on the market:

- Business Decisions and Rules Management Systems
- Predictive Analytics Tools
- Complex Event Processing and Real-Time Intelligence Tools
- Decision Modeling Tools
- Decision Optimization
  - <u>Constraint Programming Solvers</u>
  - Linear Programming Tools
- Business Process Management Software

#### www.decision-tools.org

### Live Catalogues of Optimization Tools

Contains detailed profiles of open source and commercial tools:

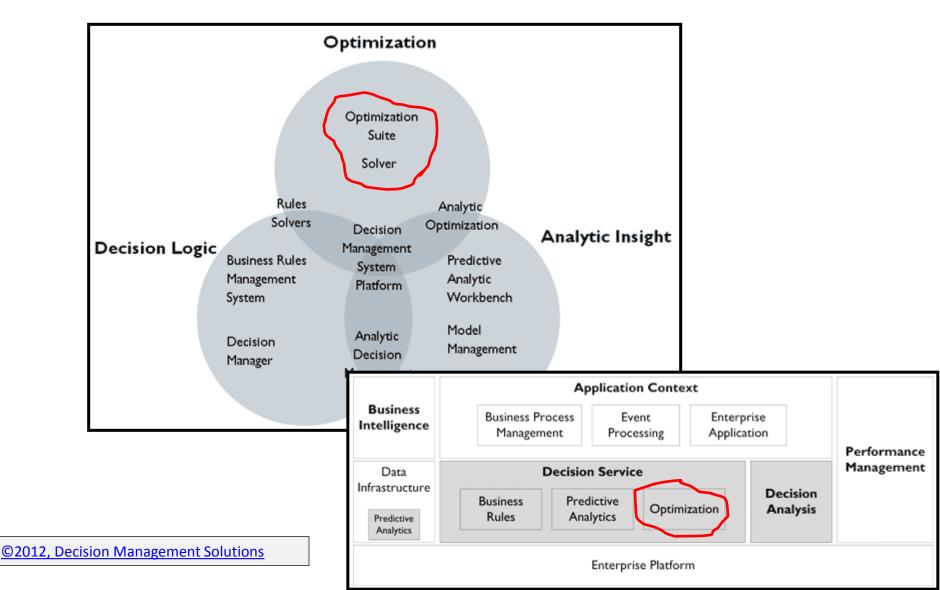
- 30 Constraint Solvers
- 11 Linear Solvers

Tool profiles are maintained by their authors

Constraint	Programming Solvers —			Sponsored by:	ACP	<b>CP</b> 20	013	Decisio CAM 201	<b>P</b> 3	OPE RUL	N S	Decis Manage Too		
					Catalogue of Cous	traint Programming 1	Fools							
s catalogue contains details submitten have an exclusi clicking on the butten "As		e this web ation shou d keep the	site. t their tools. m in the up-to-dal											
hort Catalogue									1	1				
Product Name	Brief Description	Website, Forum	Implementation Language	Modeling Language	Support of Scheduling, Routing,	Integration with LP/MIP/SAT tools	Solver Competitions, Awards	License, Pricing	First Release Year	Latest Release Date and Number	Total Number of Downloads	Number of Commercial Users	Submitted By	L
	The Airma package integrates extendily supplied solution algorithms for mathematical programming and constraint programming with model development, application integration, and application deployment.	Website Forum	Meatly C++, but also Java, Javascript and CSS are used.	ADDIS	Scheduling is supported via ACTIVITIES and RESOURCES	LP, MIP, QP, MIQP, NLP, MINLP, MCP, are supported besides CP.	ADAMS has been the optimization technology used to win the last three Franz Edelman Awards, see <u>awards</u>	Commercial, but free for seademic institutions	ADMS: 1993, ADMS-CP 2012	-	-	several	Chris Kuip Puragon Decision Technology ADDAS software developer chris.kuip@uimma.com	, ,
	AUPZ is an efficient, multi-platform modeling system based on a high- ierd algebraic medding language. It facilitates ngold development of rypimation medding languages and this medding systemistic AUPZ supports a languaristic of this medding systemic constant programming solvers and growides securitized database access.	Website Forum	C, C++	AMPL		Supports most LP and MDP solvers, as well as quadratic, nonlinear, mixed-integer quadratic and nonlinear, second-order cone and somidefinite programming, global optimization and complementarity problems.	Robert Fourer, David Gay and Brian Kernighan were awarded the 2012 DNFORMS Impact Price as the origination of one of the most important algebraic modeling languages.	Commercial, See version for seadomic courses	1985	20130625	•	many	Vietor Zverovich ANGL Software Developer viz@ampl.com	
(Cardinal)	A finite sets constraints solver (as an ECLPEs library) with especial informers on sets cardinality and other optional set functions (minimum and maximum for sets of integers, and union for sets of sets.)	Website	Prolog	Prolog	-	(ECLIPSc integration)		ECLIPSe license	2004	2005, 1.0		-	Francisco Azevedo CENTRIA, FCT, Universidado Nova de Lisboa Assistant Professor fraz@fictual.pt +351-212948536	: :
(Casper)	Constraint Solving Platform for Engineering and Research	Website	C++	C++	-	-	Third International CSP Solver Competition	Apache License	2003	-		-	Marco Correis CENTRIA - FCT/UNL Research member marco.v.correis@gmail.com	T
(Ghoso)	CHOCO is a jurn library for constraint satisfaction problems (CSP) and constraint programming (CP).	Website	Java	Choco, MiniZine	Scheduling (Cumulative, Diffn, Regular) Routing (Circuit, Subcircuit, Tree, Grapha)	Explanation Engine		BSD (fee)	1999	March 2013, Choco 13- 03 (bots version of Choco 3.0)	>59190 since 2004		Charles Prad Homme Ecole des Mines de Nantes Research Engineer choco@mines-nantes.&	2
(Chuffes)	A state of the an lazy clause solver designed from the ground up with lazy clause generation in mind	-	C++	MiniZine	•	LP propagator, built in SAT solver	•	closed source	-	-	•	•	Geoffrey Chu University of Melbourne Research Fellow chu.geoffrey@gmail.com	
(Congrete)	Concrete is a black-box CSPA solving API for the IVM, with the Scala and Java languages in mind.	Website	Seala	Scala, Java, and XCSP 2.1	-	-	Participed in CPAI07, CPAI08 and CSC09 competitions under the name CSP4J.	LGPL	2007			-	fulien Vien LAMB CNRS, Universit&D d Valencience et du Hainaut- Combr&Csis Assistant Professor julien.vien@univ- valencience.fe	•
(Cooris)	Copili is a constraint programming DSL (Domain-Specific Language) embedded in Seala. A SAT-Saced constraint softwar Sugaris used as a back-and constraint softwar.	Website	Scala	Smin	•	Integrated with Sugar and Sa4j (Java based SAT solver). Any SAT solver secepting DDAACS CNF format can be used.	•	BSD 3-Clause License	2011	September 1, 2013. Version 2.2.0	•		Naoyuki Tamuna Kobo University, Japan Professor tamuna_at_kobo-u.ac.jp +81-78-803-8364	
(Gream)	Cream is a library for constraint programming in Java.	Webaite	Java	Java				LG91	2003	January 24, 2009. Version 1.06	About 6000 since 2003.		Nacyuki Tamura Kobo University, Japan Professor tamura_at_kobo-u.as.jp 481-78-803-8364	\$
(EQUIPSE)	Constraint Logic Programming system, consisting of suntime core, collection of libraries, meddling and control language, development servicement, host language interfaces, and interfaces to third-party selvers.	Website Forum	C, Prolog	ECLiPSe Extended Prolog, Minisine		Tight LP/MP integration with Cplex, Xpress-MP, CODI-OR and Gurebi		Open Source, Mosilla Public Liernee	1992	2013, 6.1	>10000	several	Feachim Schimpf Coninfer Ltd Director info@coninfer.com	Ĩ
(Geccole)	An agus sauna C++ assentaint salvar	Website <u>Forum</u>	C++	C++, MiniZine, AMPL	schoduling bin packing		all gold modals in all estegories at MiniZine challenges 2008-2012	Open Seurce MIT license	2005	2013, 4.2.0	more than 40000, also included in Linux distributions (Debian, Ubuntu, Genteo, OpenSUSE, ) and FreeBSD		Christian Schulte Geoode Team development lead schulte@geoode.org	4
(IBM CSP Solver)	-	•					•		•		-	•	Vacl Ben-Haim VAELBH©il.ibm.com	
IBM ILOG CP Optimizer)	But BLOG DD Optimizer is medical developments and excession of programmer for which are a standards and a promotion problem. Special any physical is plotted on modeling and promotion problems, and promotion and promotion and promotion and promotion and any promotion of the problem and the properties of the problem and the prob	Website Forum	c	095, C++, Jana, C#	Support of scheduling (disjunctive teamlattive scheduling, alternative resources imodes teagles, projects woch-breakdown structures, temperal costs unch as celluters lundiness, non-encoution costs, resource allo easier costs,) and routing (requence vasibles, manition distances, transition encopression)	BM ILOG CP Optimizer is a component of IBM ILOG CPLEX Optimization Studie that also contains CPLEX Optimizer for DrMMP (OP) CCP. CP Optimizer can be tightly integrated with CPLEX Optimizer in user applications.		Commercial, but <u>free</u> for sendemic use	CP Optimize 1.0, May 2007	CPLEX Optimization Studie V12.5.1, June 2013	-		Philippe Labonie IBM Phinopel Scientist Jabonie Scientist	



### Decision Optimization within Decision Management Platforms





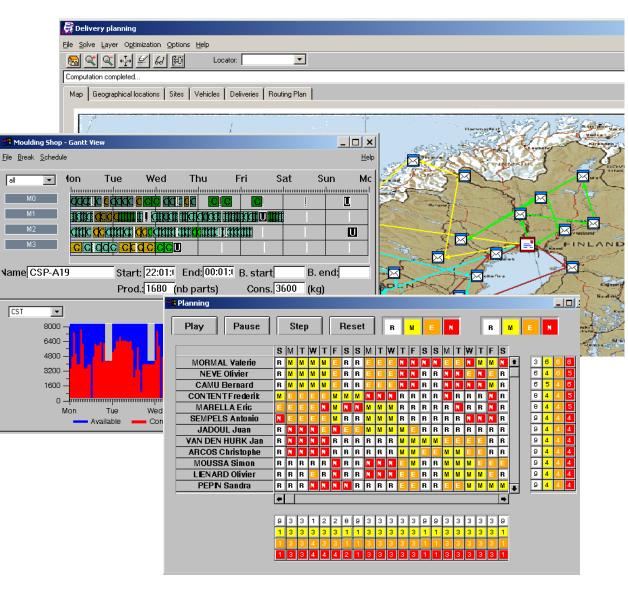
## **Decision Optimization**

- <u>Decision Optimization</u> helps *business* people to:
  - make *better decisions* subject to different *business* and *time* constraints
  - consider alternative decisions
  - find *optimal* (or close to optimal) decisions
- <u>Finds the *best* possible resource utilization</u> to achieve a desired optimization objective such as:
  - minimizing expenses or travel time
  - maximizing ROI or service level
- <u>Relies on proven mathematical techniques</u> such as:
  - Constraint Programming (CP) and Linear Programming (LP)
  - Integrated in modern decision modeling frameworks



# **Typical Optimization Applications**

- Scheduling and Resource Allocation
- Complex
   Configuration
   Problems
- Supply Chain Management
- Staff Rostering
- Vehicle Routing





### **Constraint Satisfaction Problem - CSP**

- CSP represents a decision optimization problems defining *decision variables* subject to *constraints*
- Typical CSP structure:

#### 1. Problem Definition (<u>what</u> to do)

- a. Define Decision Variables with all possible values
- b. Define Constraints on the decision variables

#### 2. Problem Resolution (<u>how</u> to do it)

- a. Find Solution(s) that defines a value for each variable such that all constraints are satisfied or
- b. Find an optimal solution that minimizes/maximizes a certain objective (a function of decision variables)



## JSR-331 "Java CP API" Standard

- JSR-331 "Java Constraint Programming API" an official Java Community Process (JCP) standard <u>www.jsr331.org</u>
- JSR-331 covers key concepts and design decisions related to the standard representation and resolution of constraint satisfaction and optimization problems
- Utilizes de-facto standardized decisions from multiple CP solvers
- JSR-331 current implementations:
  - 4 CP-based solvers
  - 6 LP-based solvers

### Simple CSP in Java (JSR-331)

```
public static void main(String[] args) {
    // ==== PROBLEM DEFINITION =======
    Problem p = ProblemFactory.newProblem("Test");
    // ====== Define variables
    Var x = p.variable("X", 1, 10);
    Var y = p.variable("Y", 1, 10);
    Var z = p.variable("Z", 1, 10);
    Var cost = x.multiply(3).multiply(y).minus(z.multiply(4));
    // ====== Define and post constraints
    p.post(x, "<", y); // X < Y
    p.post(x.plus(y), "=", z); // X + Y = Z
    // === PROBLEM RESOLUTION =======
    p.log("=== Find Solution:");
    Solver solver = p.getSolver();
    Solution solution = solver.findSolution();
    if (solution != null)
        solution.log();
                                  Solution solution = solver.findOptimalSolution(cost);
    else
        p.log("No Solution");
    p.log("Cost " + cost);
}
```



## Moving From Java to Business Decision Modeling

- Building business-oriented decision modeling facilities on top of the JSR-331
- Allowing business analysts <u>to define</u> a decision optimization problem
  - Using business concepts and decision variables (glossary)
  - Using predefined or custom constraints oriented to business people
- Relying on the standard solvers *to solve* the problem
- OpenRules<sup>®</sup> <u>Rule Solver</u> provides a decision optimization environment using intuitive decision tables managed in Excel or Google Docs



### Example: Where is Zebra?

1. There are five houses					
2. The Englishman lives in the red house					
3. The Spaniard owns the dog					
4. Coffee is drunk in the green house					
5. The Ukrainian drinks tea					
6. The green house is immediately to the right of the ivory house					
7. The Old Gold smoker owns snails					
8. Kools are smoked in the yellow house					
9. Milk is drunk in the middle house					
10. The Norwegian lives in the first house					
11. The man who smokes Chesterfields lives in the house next to the man with the fox					
12. Kools are smoked in the house next to the house where the horse is kept					
13. The Lucky Strike smoker drinks orange juice					

14. The Japanese smokes Parliaments

15. The Norwegian lives next to the blue house



### Glossary

	Decision Variables	Business Concept	Attribute	Domain	Unknown
Colors	green		green	0-4	TRUE
	ivory		ivory	0-4	TRUE
	blue		blue	0-4	TRUE
	red	1	red	0-4	TRUE
	yellow	1	yellow	0-4	TRUE
	Norwegian	1	norwegian	0-4	TRUE
	Ukrainian	1	ukrainian	0-4	TRUE
People	Japanese	1	japanese	0-4	TRUE
	Englishman	]	englishman	0-4	TRUE
	Spaniard	]	spaniard	0-4	TRUE
Drinks	juice		juice	0-4	TRUE
	tea	Zebra Problem	tea	0-4	TRUE
	milk		milk	0-4	TRUE
	water		water	0-4	TRUE
	coffee		coffee	0-4	TRUE
	snail		snail	0-4	TRUE
	dog		dog	0-4	TRUE
Pets	fox		fox	0-4	TRUE
	horse		horse	0-4	TRUE
	ZEBRA		zebra	0-4	TRUE
	Chesterfield	]	chesterfield	0-4	TRUE
	Parliament		parliament	0-4	TRUE
Cigarette	Lucky		lucky	0-4	TRUE
	OldGolds		oldGolds	0-4	TRUE
	Kools		kools	0-4	TRUE



### Decision "FindZebra"

Decision FindZebra	
Decisions	Execute Rules
All Diff Constraints	:= AllDiffConstraints()
Zebra Constraints 1	:= ZebraConstraints1()
Zebra Constraints 2	:= ZebraConstraints2()



## All Different Constraints

DecisionTable AllDiffConstraints					
ActionAllDiff					
Variables					
green,ivory,blue,red,yellow					
Norwegian, Ukrainian, Japanese, Englishman, Spaniard					
juice,tea,milk,water,coffee					
snail,dog,fox,horse,ZEBRA					
Chesterfield, Parliament, Lucky, OldGolds, Kools					



### Zebra Constraints 1

DecisionTable Zebr	aConstraints tionXoperY		
Х	<oper> Y</oper>		
Englishman	=	red	The Englishman lives in the red house
Spaniard	=	dog	The Spaniard owns the dog
coffee	=	green	Coffee is drunk in the green house
Ukrainian	=	tea	The Ukrainian drinks tea
OldGolds	=	snail	The Old Golds smoker owns snails
Kools	=	yellow	Kools are smoked in the yellow house
milk	=	2	Milk is drunk in the middle house
Norwegian	=	0	The Norwegian lives in the first house
Lucky	=	juice	The Lucky Strike smoker drinks orange juice
Japanese	=	Parliament	The Japanese smokes Parliament



### Zebra Constraints 2

DecisionTable ZebraConstraints2	
ActionConstraint	
Constraint	
<pre>{     Var green = getVar("green");     Var ivory = getVar("ivory");     solver().linear(green,"=",ivory.plus(1)); }</pre>	The green house is immediately to the right of the ivory house
<pre>{     Var Chesterfield = getVar("Chesterfield");     Var fox = getVar("fox");     Constraint right = linear(Chesterfield,"=",fox.plus(1));     Constraint left = linear(Chesterfield,"=",fox.minus(1));     right.or(left); }</pre>	The man who smokes Chesterfields lives in the house next to the man with the fox
<pre>{     Var horse = getVar("horse");     Var Kools = getVar("Kools");     Constraint right = linear(Kools,"=",horse.plus(1));     Constraint left = linear(Kools,"=",horse.minus(1));     right.or(left); }</pre>	Kools are smoked in the house next to the house where the horse is kept.
{     Var Norwegian = getVar("Norwegian");     Var blue = getVar("blue");     linear(Norwegian,"=",blue.plus(1)).or(         linear(Norwegian,"=",blue.minus(1)) ); }	The Norwegian lives next to the blue house



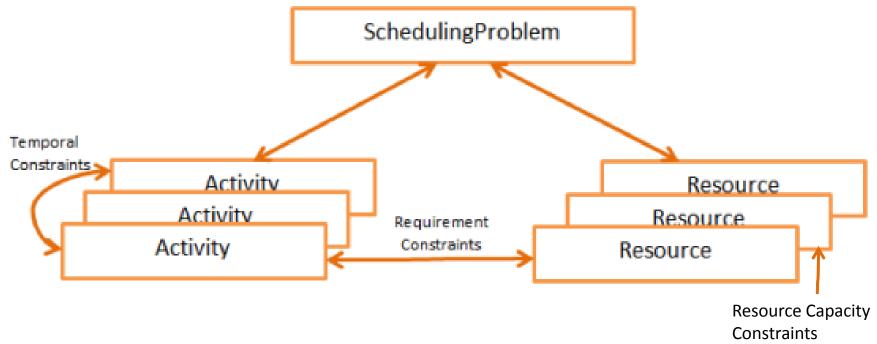
### Zebra Execution Results

House #1: fox yellow Kools water NorwegianHouse #2: Chesterfield Ukrainian horse tea blueHouse #3: OldGolds milk red Englishman snailHouse #4: Lucky juice ivory Spaniard dogHouse #5: Parliament Japanese ZEBRA green coffee



## OpenRules<sup>®</sup> Rule Solver

- Includes decision table templates for various binary and global constraints
- Includes decision table templates for scheduling and resource allocation problems:



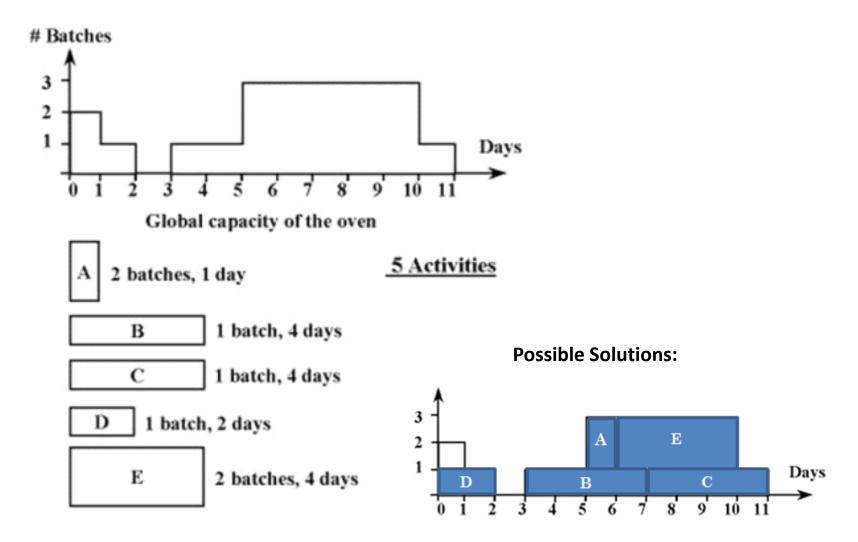


## Real-world Resource Allocation Decisions

- Many service providers have to make every day decisions by allocation their limited capacity resources to satisfy various customer requests
- Let's consider a small business that fires batches of bricks in one or several ovens (a resource with a limited capacity)
- This business has to make resource allocation decisions on a constant basis by allocating their limited resources to customer orders while satisfying scheduling and resource constraints



## Example of a Resource Allocation Problem





## Decision "DefineOvenSchedule"

#### This decision consists of 5 sub-decisions:

Decision DefineOvenSchedule			
Decisions	Execute Rules		
Define Schedule	:= DefineSchedule()		
Define Activities	:= DefineActivities()		
Define Oven as Recoverable Resource	:= DefineOvenAsResource()		
Define Oven Availability	:= SetOvenCapacities()		
Define Resource Requirement Constraints	:= ResourceRequirementConstraints()		



### **Define Schedule and Activities**

5 Activities

Decision Table Define Schedule ActionSchedule						
Origin Horizon						
0	11					

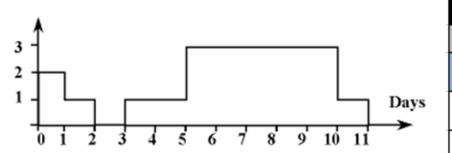
days
days
4 days

DecisionTable DefineActivities						
ActionAddActivity						
Name	Duration					
Α	1					
В	4					
С	4					
D	2					
E	4					



## Define Oven and its Availability

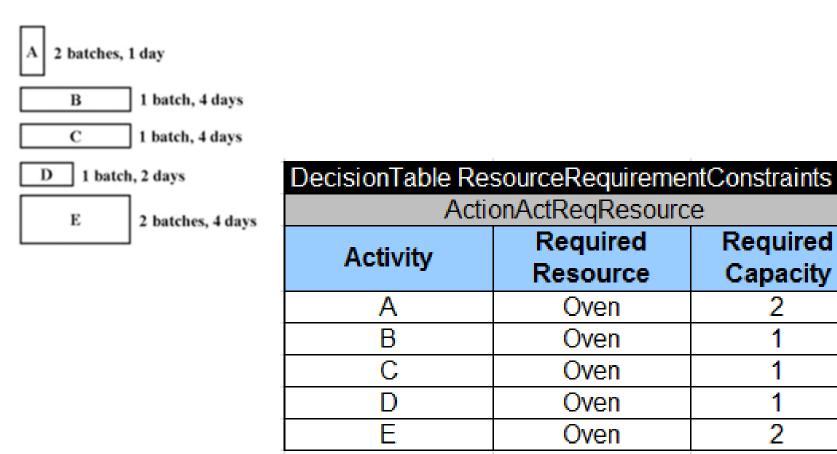
DecisionTable DefineOvenAsResource								
ActionAddResource								
Name	Max Capacity							
Oven	Recoverable	3						



DecisionTable SetOvenCapacities							
ActionResourceCapMax							
Resource	From	То	Capacity				
Oven	0	1	2				
Oven	1	2	1				
Oven	2	3	0				
Oven	3	5	1				
Oven	5	10	3				
Oven	10	11	1				



### **Define Resource Requirements**



Required

Capacity

2

2

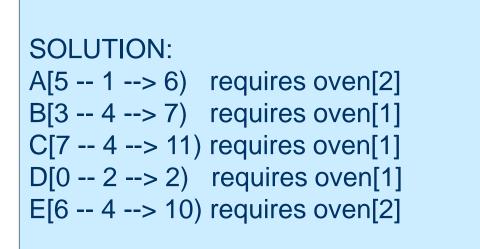


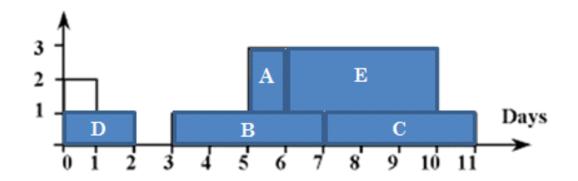
# Run Decision from Java to Find <u>One</u> Feasible Solution

```
public class Main {
    public static void main(String[] args) {
        String fileName = "file:rules/Decision.xls";
        System.setProperty("OPENRULES_MODE", "Solve");
        Decision decision = new Decision("DefineOvenSchedule",fileName);
        decision.execute();
    }
}
```



### **One Feasible Solution**







# Run Decision from Java to Find <u>ALL</u> Feasible Solutions

```
public class Main {
    public static void main(String[] args) {
        String fileName = "file:rules/Decision.xls";
        System.setProperty("OPENRULES_MODE", "Solve");
        Decision decision = new Decision("DefineOvenSchedule",fileName);
        <u>decision.put("MaxSolutions", "10");
        decision.execute();
    }
}</u>
```



### All Feasible Solutions

Solution 1:

A[5 -- 1 --> 6) requires Oven[2] B[3 -- 4 --> 7) requires Oven[1] C[7 -- 4 --> 11) requires Oven[1] D[0 -- 2 --> 2) requires Oven[1] E[6 -- 4 --> 10) requires Oven[2] Solution 2:

- A[5 -- 1 --> 6) requires Oven[2]
- B[7 -- 4 --> 11) requires Oven[1]
- C[3 -- 4 --> 7) requires Oven[1]
- D[0 -- 2 --> 2) requires Oven[1]
- E[6 -- 4 --> 10) requires Oven[2]

Solution 3:

A[9 -- 1 --> 10) requires Oven[2] B[3 -- 4 --> 7) requires Oven[1] C[7 -- 4 --> 11) requires Oven[1] D[0 -- 2 --> 2) requires Oven[1] E[5 -- 4 --> 9) requires Oven[2] Solution 4:

- A[9 -- 1 --> 10) requires Oven[2]
- B[7 -- 4 --> 11) requires Oven[1]
- C[3 -- 4 --> 7) requires Oven[1]
- D[0 -- 2 --> 2) requires Oven[1]
- E[5 -- 4 --> 9) requires Oven[2]



## Another Real-World Example "Workforce Management"

- Workforce management is central to efficient operations and good customer service.
- Proper scheduling of employees can mean the difference between profitability and business failure.
- As the manager, you are required to hire and set the weekly work schedule for your employees.



## Employee Scheduling Requirements

- The required levels for the week are as follows:
  - Total employees required

Mon	Tue	Wed	Thu	Fri	Sat	Sun
5	8	9	10	16	18	12

Available employees:

Employee Type	Total	Cost per Day
F/T	14	\$100
P/T	4	\$150

Possible Solution:

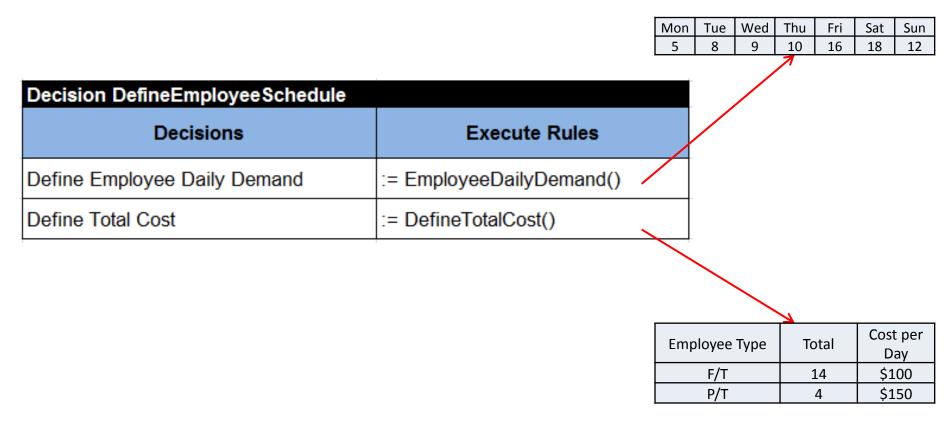
	Μ	Т	W	Т	F	S	S
FT	5	8	9	10	14	14	12
PT	0	0	0	0	2	4	0

• Assuming the same staffing requirements continue week after week, what is the minimal staffing cost?



### Decision "DefineEmployeeSchedule"

- Start with a decision
- Presented in Excel using OpenRules Rule Solver





### **Decision's Glossary**

- Decision Variables
- For each day one for FT and one for PT

Glossary glossary	2			
Decision Variable	Business Concept	Attribute	Domain	Unknown
Mon FT		monFT	0-14	TRUE
Mon PT		monPT	0-4	TRUE
Tue FT		tueFT	0-14	TRUE
Tue PT		tuePT	0-4	TRUE
Wed FT		wedFT	0-14	TRUE
Wed PT		wedPT	0-4	TRUE
Thu FT		thuFT	0-14	TRUE
Thu PT	Roster	thuPT	0-4	TRUE
Fri FT	]	friFT	0-14	TRUE
Fri PT		friPT	0-4	TRUE
Sat FT		satFT	0-14	TRUE
Sat PT	]	satPT	0-4	TRUE
Sun FT	]	sunFT	0-14	TRUE
Sun PT	]	sunPT	0-4	TRUE
Total Cost		totalCost	0-20000	TRUE

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### Decision Table "EmployeeDailyDemand"

<b>Decision</b> Tabl	e Emple	oyeeDailyDe	mand	
	Actio	nXoperYcomp	oareZ	
Variable	Arith Oper	Variable	Compare Oper	Value
Mon FT	+	Mon PT	=	5
Tue FT	+	Tue PT	=	8
Wed FT	+	Wed PT	=	9
Thu FT	+	Thu PT	=	10
Fri FT	+	Fri PT	=	16
Sat FT	+	Sat PT	=	18
Sun FT	+	Sun PT	=	12

Mon	Tue	Wed	Thu	Fri	Sat	Sun
5	8	9	10	16	18	12



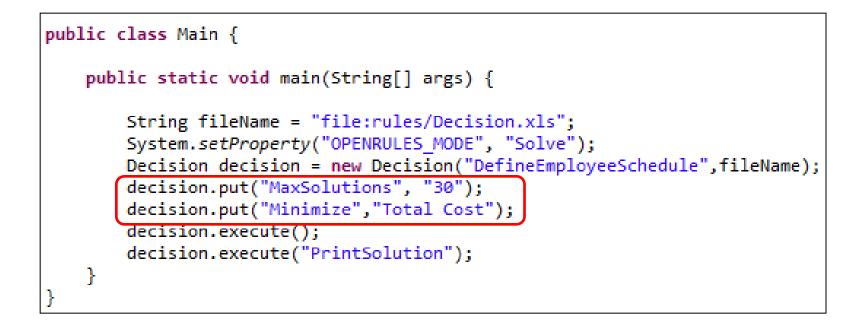
### Decision Table "DefineTotalCost"

Decision Table Define TotalCost						
	ActionScalProd					
Name of the Scalar Product Numbers Variables						
Total Cost	100,150,100,150,100,150, 100,150,100,150,100,150, 100,150	Mon FT, Mon PT, Tue FT, Tue PT, Wed FT, Wed PT, Thu FT, Thu PT, Fri FT, Fri PT, Sat FT, Sat PT, Sun FT, Sun PT				

Employee Type	Total	Cost per Day
F/T	14	\$100
P/T	4	\$150



# Run Decision from Java to Find <u>One</u> Feasible Solution





### **Decision Results**

Found a solution with Total Cost[8700] Found a solution with Total Cost[8650] Found a solution with Total Cost[8600] Found a solution with Total Cost[8550] Found a solution with Total Cost[8500] Found a solution with Total Cost[8450] Found a solution with Total Cost[8400] Found a solution with Total Cost[8350] Found a solution with Total Cost[8300] Found a solution with Total Cost[8250] Found a solution with Total Cost[8200] Found a solution with Total Cost[8150] Found a solution with Total Cost[8100] Found a solution with Total Cost[8100] \*\*\* Execution Profile \*\*\* Number of Choice Points: 94360 Number of Failures: 94333 Occupied memory: 93172496 Execution time: 14885 msec

===== Optimal Solution ======= M T W T F S S FT 5 8 9 10 14 14 12 PT 0 0 0 0 2 4 0 COST: 8100 =================================



## **Smarter Search Strategies**

- Adding time limits for:
  - Search of one solution
  - The overall search
- CP solvers provide many search strategies for selecting variables and values to try first, e.g.
  - Notorious "N-Queens" problem: using a selector MIN\_DOMAIN\_MIN\_VALUE improves performance 1,000 times
- CP/LP tools provide different optimization options that may be tried without changing a decision model



## Conclusion

- Combination of BR and CP/LP tools creates a powerful while intuitive decision modeling and optimization framework
- Many practical Decision Optimization problems may be successfully modeled and solved by subject matter experts using off-the-shelf CP/LP tools such as <u>OpenRules Rule Solver</u>
- The <u>JSR-331</u> standard gives all BR vendors an opportunity to add a true optimization component to their product offerings



### Q&A

### Web: <u>www.OpenRules.com</u>

Email:

support@openrules.com

jacobfeldman@openrules.com